Publicly-verifiable proof of storage: a modular construction

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Proof of Storage (PoS)

A *Proofs of Storage* protocol allows a client to verify that a server is correctly storing a user's file.

A PoS protocol is *publicly-verifiable* when the verification doesn't require any secret parameter.

The parties involved are:

- The *server*, who stores the file.
- The user, who wants to store the file.
- A verifier, who checks that the file is being stored by the server.

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- Secrecy of the stored file. The server can read any part of the file: a user must encrypt the file to maintain privacy.
- **Retrieving the file.** The server can refuse to give back the file to the user but still pass the verification, because it is actually storing the file.
- Recovering a partially corrupted file. Part of the stored file can become corrupted. The PoS protocol detects the problem, but doesn't restore the file.

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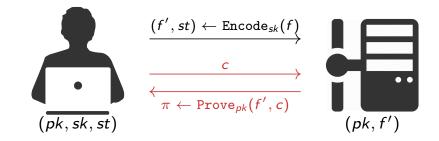
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We can trivially obtain a PoS protocol if the user stores a hash h of its file f and the server sends back the whole file, f'.

Verify(f'): if H(f') == h return *true*; else return *false*;

We require the protocol be efficient in term of bandwidth: the communication complexity must be much lower than the size of the file.

- **Cloud storage:** the user can verify that their files are correctly stored by the cloud provider: otherwise the server might remove files that are unlikely to be accessed (e.g., old backups).
- Automated, trustless payment for file storage: with public verifiability a trusted third party (or a smart contract) can verify that the server is storing the file and authorize the payment, without requiring any trust between the user and the server.



$$b = \text{Verify}_{pk}(st, c, \pi)$$

The protocol is *correct*:

The server knows $f' \implies$ the verification succeeds.

The protocol is secure:

 \mathcal{A} can verify \implies we can "extract" the file f from \mathcal{A} .

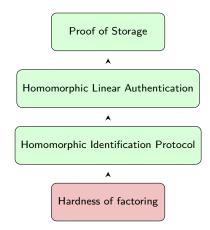
Ateniese, Kamara, Katz - ASIACRYPT 2009

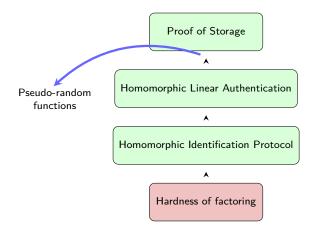
We can build a correct and secure *publicly-verifiable PoS protocol* based on the hardness of factoring in the random oracle model.

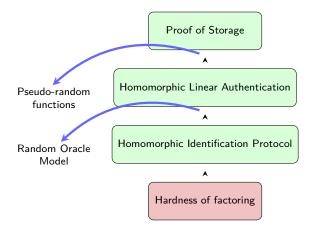
- Unlimited challenges.
- Public verifiability.

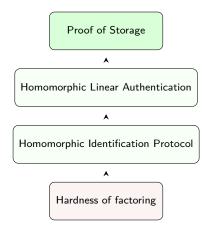
And with respect to the file size:

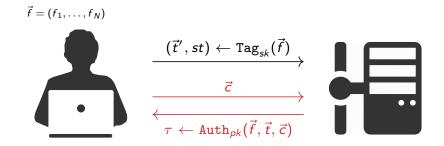
- Communication complexity: $\mathcal{O}(1)$.
- Server storage: the file f and a overhead $\mathcal{O}(1)$.
- Client storage: $\mathcal{O}(1)$.











$$b = \texttt{Verify}_{pk}(st, \mu, \vec{c}, \tau)$$

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Correctness

$$ext{Verify}_{pk}\left(st,\sum_i c_i f_i, ec{c}, au
ight) = 1$$

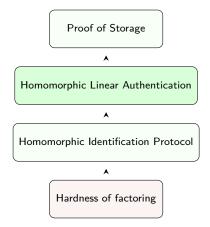
Security

A polynomial adversary cannot forge a valid authentication proof for $\mu \neq \sum_{i} c_i f_i$.

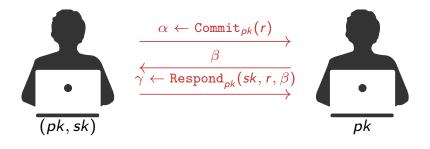
The file is split: $\vec{f} = (f_1, \dots, f_N)$, with $f_i \in \mathbb{Z}_p$. The server stores a file with HLA tags: $\vec{f}' = (\vec{f}, \vec{t})$.

The request procedure consists in:

- Share a key K for the pseudo-random function F: the commitment is $c_i = F_K(i) \in \mathbb{Z}_p$.
- Using the HLA protocol we compute $\tau \leftarrow \text{Auth}_{pk}(\vec{f}, \vec{t}, \vec{c})$ and set $\mu = \sum_{i} f_i c_i$. The PoS proof is $\pi = (\mu, \tau)$.
- To verify we use Verify of the HLA protocol.



Verify that the user knows the secret key sk without revealing additional information.



$$b = \operatorname{Verify}_{pk}(\alpha, \beta, \gamma)$$

For an homomorphic protocol we add Combine₁ and Combine₃.

Correctness If $\{(\alpha_i, \beta_i, \gamma_i)\}_{i=1}^n$ is a set of valid IP transcript (Verify = 1) and \vec{c} is a vector: $\operatorname{Verify}_{pk}\left(\operatorname{Combine}_1(\vec{c}, \vec{\alpha}), \sum_i c_i \beta_i, \operatorname{Combine}_3(\vec{c}, \vec{\gamma})\right).$

Security

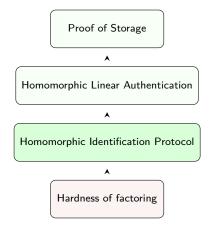
A polynomial adversary ${\cal A}$ has negligible probability to output a string (\vec{c},μ',γ') such that:

•
$$\mu' \neq \sum_i c_i \beta_i$$
.

• Verify_{pk} (Combine₁(
$$\vec{c}, \vec{lpha}$$
), μ', γ') = 1.

The file is split: $\vec{f} = (f_1, \ldots, f_N)$, with $f_i \in \mathbb{Z}_p$. Implicitly $\beta_i = f_i$.

$$\begin{split} & \operatorname{Tag}_{sk}(\vec{f}) \colon \text{We take a random element } st \text{ and we fix } r_i = H(st,i) \text{ and} \\ & \alpha_i = \operatorname{Commit}_{pk}(r_i). \text{ We compute } \gamma_i = \operatorname{Respond}_{pk}(sk, r_i, f_i). \\ & \operatorname{The tag is } \vec{t} = (\gamma_1, \ldots, \gamma_n). \\ & \operatorname{Auth}_{pk}(\vec{f}, \vec{t}, \vec{c}) \colon \text{Output the combined tag } \tau = \operatorname{Combine}_3(\vec{c}, \vec{t}). \\ & \operatorname{Verify}_{pk}(st, \mu, \vec{c}, \tau) \colon \text{Output the combined verification} \\ & \operatorname{Verify}_{pk}(\operatorname{Combine}_1(\vec{c}, \vec{\alpha}), \mu, \tau). \end{split}$$



Quadratic residuosity: N = pq, \mathcal{J}_N^{+1} is the set of element in \mathbb{Z}_N with Jacobi symbol +1, and \mathcal{QR}_N is the set of quadratic residues mod N.

$$y \stackrel{\$}{\leftarrow} \mathcal{QR}_N; \ pk = (N, y); \ sk = (p, q).$$

$$\begin{split} & \operatorname{Commit}_{pk}(r) \colon \operatorname{output} \alpha = r \text{ as element of } \mathcal{J}_N^{+1}.\\ & \operatorname{Respond}_{pk}(sk,r,\beta) \colon \operatorname{output} \gamma, \text{ a random } 2^{3k}\text{-th root of } \pm ry^{\beta}.\\ & \operatorname{Verify}_{pk}(\alpha,\beta,\gamma) \colon \operatorname{output} 1 \text{ if and only if } \gamma^{2^{3k}} = \pm \alpha y^{\beta} \text{ and } \beta < 2^{3k}.\\ & \operatorname{Combine}(\vec{c},\vec{x}) \colon \operatorname{output} \prod_i x_i^{c_i}. \end{split}$$

Thank you for your attention.