

Penvelope

Version 1.0

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Chapter 1

Penvelope

1.1 The functions

1.1.1 PEnvelopingAlgebra

◇ `PEnvelopingAlgebra(L)` (operation)

Here L is a restricted Lie algebra. This function returns the p -enveloping algebra of L .

It is possible to add the option `cut`, as in `PEnvelopingAlgebra(L : cut)`; In this case the quotient of the p -enveloping algebra by the $c + 1$ -st power of the Jacobson radical will be returned. In this case the Lie algebra has to be graded.

Example

```
gap> L:= JenningsLieAlgebra(H1);
<Lie algebra of dimension 6 over GF(3)>
gap> U:= PEnvelopingAlgebra( L : cut );
<algebra of dimension 75 over GF(3)>
```

1.1.2 QuotientByMaximalIdeal

◇ `QuotientByMaximalIdeal(U)` (operation)

Here U must be a p -enveloping algebra. This function returns a list of two elements. The first is an associative algebra isomorphic to a quotient of U (the ideal is constructed by taking consecutive complements to the Lie algebra inside subspaces consisting of u such that $Uu = uU = 0$). The second element of the list is a set of basis elements that form a basis of the Lie algebra inside the algebra.

Example

```
gap> U:= PEnvelopingAlgebra( L : cut );
<algebra of dimension 26 over GF(3)>
gap> QuotientByMaximalIdeal( U );
[ <algebra of dimension 9 over GF(3)>, [ v.2, v.3, v.4, v.5, v.6, v.7 ] ]
```

1.1.3 UElement

◇ `UElement(a)` (operation)

Here a is a nilpotent element of a ring, for example a p -enveloping algebra. This function returns the invertible element $1+a$.

Example

```
gap> L:= JenningsLieAlgebra( H2 );
<Lie algebra of dimension 6 over GF(3)>
gap> U:= PEnvelopingAlgebra( L : cut );
<algebra of dimension 23 over GF(3)>
gap> r:= QuotientByMaximalIdeal( U );
[ <algebra of dimension 10 over GF(3)>, [ v.2, v.3, v.4, v.5, v.6, v.7 ] ]
gap> UElement( r[2][1] );
1 + v.2
```

1.1.4 PCGroupByUElements

◇ `PCGroupByUElements(list)`

(operation)

Here `list` is a list of elements made by `UElement`. This function returns a pc group isomorphic to the group generated by the elements in `list`.

Example

```
gap> h:= List( r[2], UElement );
[ 1 + v.2, 1 + v.3, 1 + v.4, 1 + v.5, 1 + v.6, 1 + v.7 ]
gap> PCGroupByUElements( h{[1,2]} );
#I default 'IsGeneratorsOfMagmaWithInverses' method returns 'true' for
[ 1 + v.2, 1 + v.3 ]
The size of G is 9
Group([ f1, f2 ])
```

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