$$
\begin{aligned}
\dot{L}_{Q}^{I N}= & \frac{r^{T}}{1+s^{T} T_{F_{1}}^{I N}} \sigma^{A} A_{F_{1}}^{I N}-\beta_{1}^{L} H_{1}^{I N} L_{Q}^{I N}-d^{L} L_{Q}^{I N} \\
\dot{L}_{Q}^{O U T}= & \frac{r^{T}}{1+s^{T} T_{F_{1}}^{O U T}} \sigma^{A} A_{F_{1}}^{O U T}+\frac{r^{T}}{1+s^{T} T_{F_{2}}^{O U T} \sigma^{A} A_{F_{2}}^{O U T}-\left(\beta_{1}^{L} H_{1}^{O U T}+\beta_{2}^{L} H_{2}\right) L_{Q}^{O U T}-d^{L} L_{Q}^{O U T}} \\
\dot{L}_{F_{1}}^{I N, e}= & \beta_{1}^{L} L_{Q}^{I N} H_{1}^{I N, i}+\beta_{1}^{L} L_{Q}^{I N}\left(H_{1}^{I N, s}+H_{1}^{I N, r}\right)\left(1-\exp \left\{-\frac{\lambda N_{F_{1}}^{I N, i}}{H_{1}^{I N}}\right\}\right)+ \\
& -\sigma^{L} L_{F_{1}}^{I N, e}-\rho L_{F_{1}}^{I N, e}+\rho L_{F_{1}}^{O U T, e} \\
\dot{L}_{F_{1}}^{O U T, e}= & \beta_{1}^{L} L_{Q}^{O U T} H_{1}^{O U T, i}+\beta_{1}^{L} L_{Q}^{O U T}\left(H_{1}^{O U T, s}+H_{1}^{O U T, r}\right)\left(1-\exp \left\{-\frac{\lambda N_{F_{1}, i}^{O U T, i}}{H_{1}^{O U T}}\right\}\right)+ \\
& -\sigma^{L} L_{F_{1}}^{O U T, e}+s c a l e \rho L_{F_{1}}^{I N, e}-\text { scale } \rho L_{F_{1}}^{O U T, e} \\
\dot{L}_{F_{1}}^{I N, s}= & {\left[\beta_{1}^{L}\left(H_{1}^{I N, s}+H_{1}^{I N, r}\right) \exp \left\{-\frac{\lambda N_{F_{1}}^{I N, i}}{H_{1}^{I N}}\right\}\right] L_{Q}^{I N}-\sigma^{L} L_{F_{1}}^{I N, s}-\rho L_{F_{1}}^{I N, s}+\rho L_{F_{1}}^{O U T, s} } \\
\dot{L}_{F_{1}}^{O U T, s}= & {\left[\beta_{1}^{L}\left(H_{1}^{O U T, s}+H_{1}^{O U T, r}\right) \exp \left\{-\frac{\lambda N_{F_{1}}^{O U T, i}}{H_{1}^{O U T}}\right\}\right] L_{Q}^{O U T}+} \\
& -\sigma^{L} L_{F_{1}}^{O U T, s}+s c a l e \rho L_{F_{1}}^{I N, s}-\text { scale } \rho L_{F_{1}}^{O U T, s}
\end{aligned}
$$

$$
\begin{aligned}
& \dot{N}_{Q}^{I N, i}=m^{L} \sigma^{L} L_{F_{1}}^{I N, e}-d^{N} N_{Q}^{I N, i}-\beta_{1}^{N} H_{1}^{I N} N_{Q}^{I N, i} \\
& \dot{N}_{Q}^{\text {OUT,i }}=m^{L} \sigma^{L} L_{F_{1}}^{\text {OUT,e }}-d^{N} N_{Q}^{O U T, i}-\left(\beta_{1}^{N} H_{1}^{\text {OUT }}+\beta_{2}^{N} H_{2}\right) N_{Q}^{\text {OUT, } i} \\
& \dot{N}_{Q}^{I N, s}=m^{L} \sigma^{L} L_{F_{1}}^{I N, s}-d^{N} N_{Q}^{I N, s}-\beta_{1}^{N} H_{1}^{I N} N_{Q}^{I N, s} \\
& \dot{N}_{Q}^{\text {OUT,s }}=m^{L} \sigma^{L}\left(L_{F_{1}}^{\text {OUT,s }}+L_{F_{2}}^{\text {OUT,s }}\right)-d^{N} N_{Q}^{\text {OUT,s }}-\left(\beta_{1}^{N} H_{1}^{\text {OUT }}+\beta_{2}^{N} H_{2}\right) N_{Q}^{\text {OUT,s }} \\
& \dot{N}_{F_{1}}^{I N, i}=\beta_{1}^{N} H_{1}^{I N} N_{Q}^{I N, i}-\sigma^{N} N_{F_{1}}^{I N, i}-\rho N_{F_{1}}^{I N, i}+\rho N_{F_{1}}^{O U T, i} \\
& \dot{N}_{F_{1}}^{O U T, i}=\beta_{1}^{N} H_{1}^{O U T} N_{Q}^{O U T, i}-\sigma^{N} N_{F_{1}}^{O U T, i}+\text { scale } \rho N_{F_{1}}^{I N, e}-\text { scale } \rho L_{F_{1}}^{O U T, e} \\
& \dot{N}_{F_{1}}^{I N, e}=\beta_{1}^{N} N_{Q}^{I N, s} H_{1}^{I N, i}+\beta_{1}^{N} N_{Q}^{I N, s}\left(H_{1}^{I N, s}+H_{1}^{I N, r}\right)\left(1-\exp \left\{-\frac{\lambda N_{F_{1}}^{I N, i}}{H_{1}^{I N}}\right\}\right)+ \\
& -\sigma^{N} N_{F_{1}}^{I N, e}-\rho N_{F_{1}}^{I N, e}+\rho N_{F_{1}}^{O U T, e} \\
& \dot{N}_{F_{1}}^{O U T, e}=\beta_{1}^{N} N_{Q}^{\text {OUT,s }} H_{1}^{O U T, i}+\beta_{1}^{N} N_{Q}^{\text {OUT,s }}\left(H_{1}^{\text {OUT,s }}+H_{1}^{\text {OUT,r }}\right)\left(1-\exp \left\{-\frac{\lambda N_{F_{1}}^{O U T, i}}{H_{1}^{O U T}}\right\}\right)+ \\
& -\sigma^{N} N_{F_{1}}^{\text {OUT,e }}+\text { scale } \rho L_{N_{1}}^{I N, e}-\text { scale } \rho L_{N_{1}}^{\text {OUT,e }} \\
& \dot{N}_{F_{1}}^{I N, s}=\left[\beta_{1}^{N}\left(H_{1}^{I N, s}+H_{1}^{I N, r}\right) \exp \left\{-\frac{\lambda N_{F_{1}}^{I N, i}}{H_{1}^{I N}}\right\}\right] N_{Q}^{I N, s}-\sigma^{N} N_{F_{1}}^{I N, s}-\rho N_{F_{1}}^{I N, s}+\rho N_{F_{1}}^{O U T, s} \\
& \dot{N}_{F_{1}}^{O U T, s}=\left[\beta_{1}^{N}\left(H_{1}^{O U T, s}+H_{1}^{O U T, r}\right) \exp \left\{-\frac{\lambda N_{F_{1}, i}^{O U T, i}}{H_{1}^{O U T}}\right\}\right] N_{Q}^{O U T, s}+ \\
& -\sigma^{N} N_{F_{1}}^{O U T, s}+\text { scale } \rho N_{F_{1}}^{I N, s}-\text { scale } \rho N_{F_{1}}^{O U T, s} \\
& \dot{N}_{F_{2}}^{O U T, i}=\beta_{2}^{N} H_{2} N_{Q}^{O U T, i}-\sigma^{N} N_{F_{2}}^{O U T, i} \\
& \dot{N}_{F_{2}}^{O U T, s}=\beta_{2}^{N} H_{2} N_{Q}^{O U T, s}-\sigma^{N} N_{F_{2}}^{O U T, s}
\end{aligned}
$$

$$
\begin{aligned}
& \dot{A}_{Q}^{I N, i}=m^{N} \sigma^{N}\left(N_{F_{1}}^{I N, i}+N_{F_{1}}^{I N, e}\right)-d^{A} A_{Q}^{I N, i}-\beta_{1}^{A} H_{1}^{I N} A_{Q}^{I N, i} \\
& \dot{A}_{Q}^{\text {OUT, } i}=m^{N} \sigma^{N}\left(N_{F_{1}}^{\text {OUT,i }}+N_{F_{2}}^{\text {OUT,i }}+N_{F_{1}}^{\text {OUT,e }}\right)-d^{A} A_{Q}^{\text {OUT,i }}-\left(\beta_{1}^{A} H_{1}^{\text {OUT }}+\beta_{2}^{A} H_{2}\right) A_{Q}^{\text {OUT,i }} \\
& \dot{A}_{Q}^{I N, s}=m^{N} \sigma^{N} N_{F}^{I N, s}-d^{A} A_{Q}^{I N, s}-\beta_{1}^{A} H_{1}^{I N} A_{Q}^{I N, s} \\
& \dot{A}_{Q}^{\text {OUT,s }}=m^{N} \sigma^{N}\left(N_{F_{1}}^{\text {OUT,s }}+N_{F_{2}}^{O U T, s}\right)-d^{A} A_{Q}^{\text {OUT,s }}-\left(\beta_{1}^{A} H_{1}^{\text {OUT }}+\beta_{2}^{A} H_{2}\right) A_{Q}^{\text {OUT,s }} \\
& \dot{A}_{F_{1}}^{I N}=\beta_{1}^{A} H_{1}^{I N}\left(A_{Q}^{I N, i}+A_{Q}^{I N, s}\right)-\sigma^{A} A_{F_{1}}^{I N}-\rho A_{F_{1}}^{I N}+\rho A_{F_{1}}^{O U T} \\
& \dot{A}_{F_{1}}^{O U T}=\beta_{1}^{A} H_{1}^{O U T}\left(A_{Q}^{I N, i}+A_{Q}^{I N, s}\right)-\sigma^{A} A_{F_{1}}^{\text {OUT }}+\text { scale } \rho A_{F_{1}}^{I N}-\text { scale } \rho A_{F_{1}}^{\text {OUT }} \\
& \dot{A}_{F_{2}}^{\text {OUT }}=\beta_{2}^{A} H_{2}\left(A_{Q}^{\text {OUT,i }}+A_{Q}^{\text {OUT,s }}\right)-\sigma^{A} A_{F_{2}}^{\text {OUT }} \\
& \dot{H}_{1}^{I N, s}=r_{1} H_{1}^{I N}-d_{1}\left(H_{1}\right) H_{1}^{I N, s}-\left(\beta_{1}^{N} N_{Q}^{I N, i}+\beta_{1}^{A} A_{Q}^{I N, i}\right) H_{1}^{I N, s}+\rho H_{1}^{O U T, s}-\rho H_{1}^{I N, s} \\
& \dot{H}_{1}^{I N, i}=\left(\beta_{1}^{N} N_{Q}^{I N, i}+\beta_{1}^{A} A_{Q}^{I N, i}\right) H_{1}^{I N, s}-\left(d_{1}\left(H_{1}\right)+\gamma_{1}+\alpha_{1}\right) H_{1}^{I N, i}+\rho H_{1}^{O U T, i}-\rho H_{1}^{I N, i} \\
& \dot{H}_{1}^{I N, r}=\gamma_{1} H_{1}^{I N, i}-d_{1}\left(H_{1}\right) H_{1}^{I N, r}+\rho H_{1}^{O U T, r}-\rho H_{1}^{I N, r} \\
& \dot{H}_{1}^{\text {OUT,s }}=r_{1} H_{1}^{\text {OUT }}-d_{1}\left(H_{1}\right) H_{1}^{\text {OUT,s }}-\left(\beta_{1}^{N} N_{Q}^{\text {OUT,i }}+\beta_{1}^{A} A_{Q}^{\text {OUT,i }}\right) H_{1}^{\text {OUT,s }}+ \\
& \text { - scale } \rho H_{1}^{\text {OUT,s }}+\text { scale } \rho H_{1}^{I N, s} \\
& \dot{H}_{1}^{\text {OUT }, i}=\left(\beta_{1}^{N} N_{Q}^{\text {OUT,i }}+\beta_{1}^{A} A_{Q}^{\text {OUT,i }}\right) H_{1}^{\text {OUT,s }}-\left(d_{1}\left(H_{1}\right)+\gamma_{1}+\alpha_{1}\right) H_{1}^{\text {OUT, } i}+ \\
& \text { - scale } \rho H_{1}^{O U T, i}+\text { scale } \rho H_{1}^{I N, i} \\
& \dot{H}_{1}^{\text {OUT, } r}=\gamma_{1} H_{1}^{\text {OUT,i }}-d_{1}\left(H_{1}\right) H_{1}^{\text {OUT, } r}-\text { scale } \rho H_{1}^{\text {OUT,r }}+\text { scale } \rho H_{1}^{I N, r}
\end{aligned}
$$

